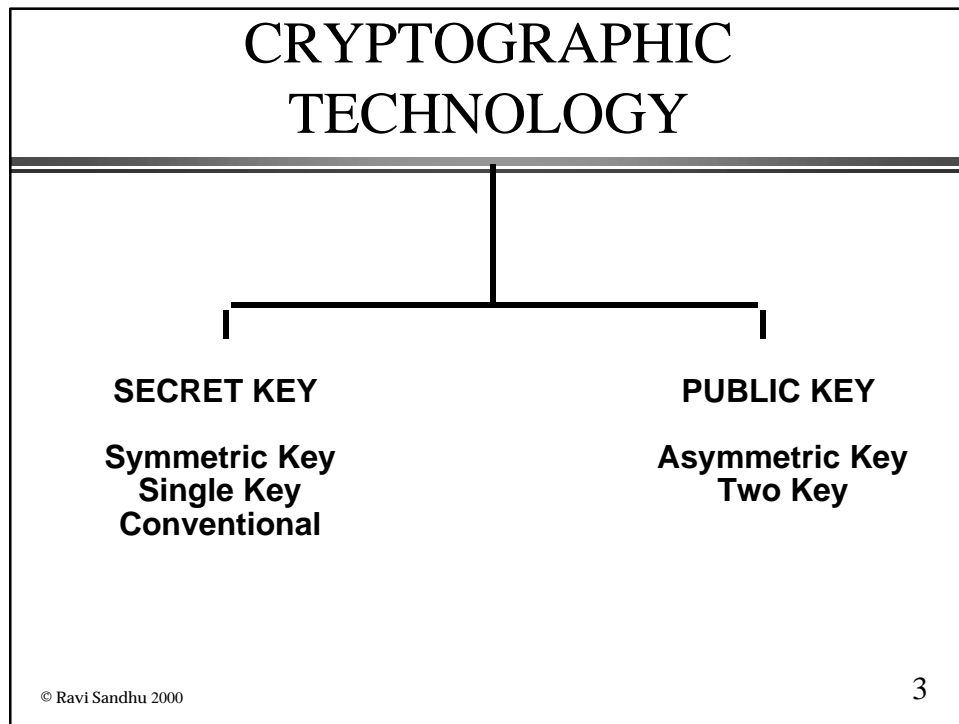


**INFS 766/INFT 865**  
**Internet Security Protocols**

**Lectures 3 and 4**  
**Cryptography in network protocols**

**Prof. Ravi Sandhu**

**CRYPTOGRAPHY**



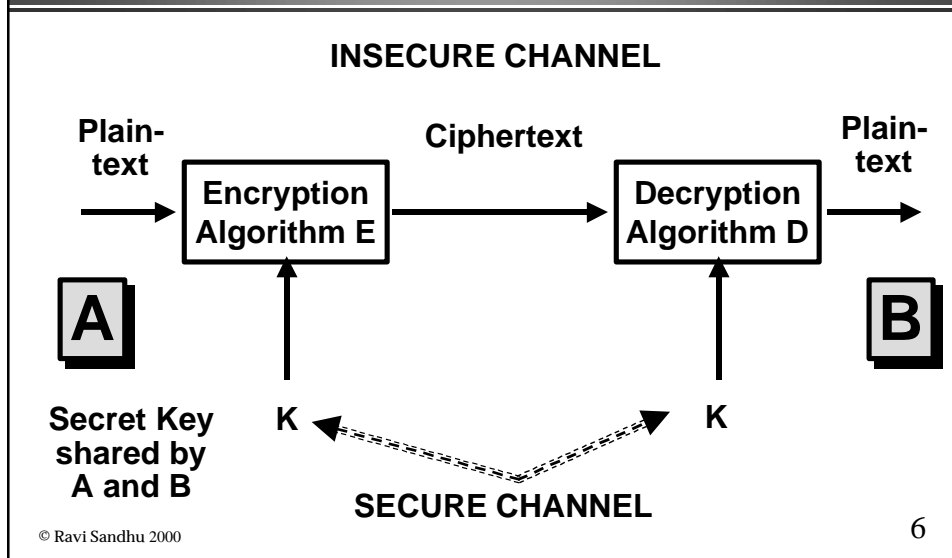
## CRYPTOGRAPHIC SERVICES

- ◆ confidentiality
  - traffic flow confidentiality
- ◆ integrity
- ◆ authentication
- ◆ non-repudiation

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## SECRET KEY CRYPTOSYSTEM



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## SECRET KEY CRYPTOSYSTEM

- ◆ **confidentiality depends only on secrecy of the key**
  - size of key is critical
- ◆ **secret key systems do not scale well**
  - with  $N$  parties we need to generate and distribute  $N*(N-1)/2$  keys
- ◆ **A and B can be people or computers**

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## MASTER KEYS AND SESSION KEYS

- ◆ **long-term or master keys**
  - prolonged use increases exposure
- ◆ **session keys**
  - short-term keys communicated by means of
    - long-term secret keys
    - public key technology

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## CRYPTANALYSIS

- ◆ ciphertext only
  - cryptanalyst only knows ciphertext
- ◆ known plaintext
  - cryptanalyst knows some plaintext-ciphertext pairs
- ◆ chosen plaintext
- ◆ chosen ciphertext

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## KNOWN PLAINTEXT ATTACK

- ◆ 40 bit key requires  $2^{39} \approx 5 * 10^{11}$  trials on average (exportable from USA)
- ◆ trials/second      time required
- 1                      20,000 years
- $10^3$                   20 years
- $10^6$                   6 days
- $10^9$                   9 minutes
- $10^{12}$                 0.5 seconds

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## KNOWN PLAINTEXT ATTACK

◆ 56 bit key requires  $2^{55} \approx 3.6 * 10^{16}$  trials on average (DES)

◆ trials/second	time required
1	$10^9$ years
$10^3$	$10^6$ years
$10^6$	$10^3$ years
$10^9$	1 year
$10^{12}$	10 hours

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## KNOWN PLAINTEXT ATTACK

◆ 80 bit key requires  $2^{79} \approx 6 * 10^{23}$  trials on average (SKIPJACK)

◆ trials/second	time required
1	$10^{16}$ years
$10^3$	$10^{13}$ years
$10^6$	$10^{10}$ years
$10^9$	$10^7$ years
$10^{12}$	$10^4$ years

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## KNOWN PLAINTEXT ATTACK

- ◆ 128 bit key requires  $2^{127} \approx 2 * 10^{38}$  trials on average (IDEA)

◆ trials/second	time required
1	$10^{30}$ years
$10^3$	$10^{27}$ years
$10^6$	$10^{24}$ years
$10^9$	$10^{21}$ years
$10^{12}$	$10^{18}$ years

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## DICTIONARY ATTACKS

- ◆ if keys are poorly chosen known plaintext attacks can be very simple
- ◆ often the user's password is the key
  - in a dictionary attack the cryptanalyst tries passwords from a dictionary, rather than all possible keys
  - for a 20,000 word dictionary, 1 trial/second will crack a poor password in less than 3 hours

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## CURRENT GENERATION SECRET KEY CRYPTOSYSTEMS

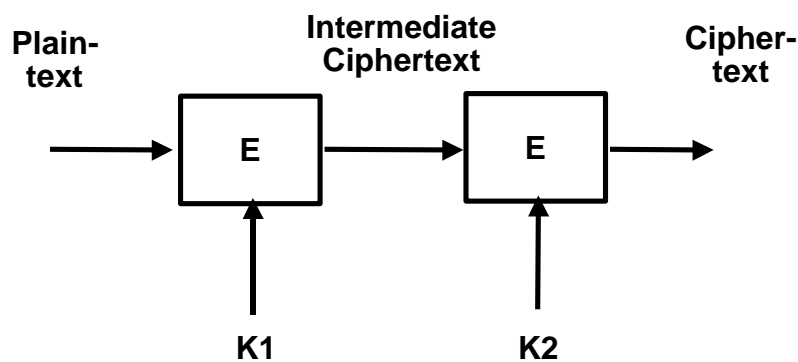
### ◆ 64 bit data block size

- DES: 56 bit key
- Triple DES: 112 bit key
- Triple DES: 168 bit key
- Skipjack: 80 bit key
- IDEA: 128 bit key
- RC2: variable size key: 1 byte to 128 bytes
- many others

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## DOUBLE DES

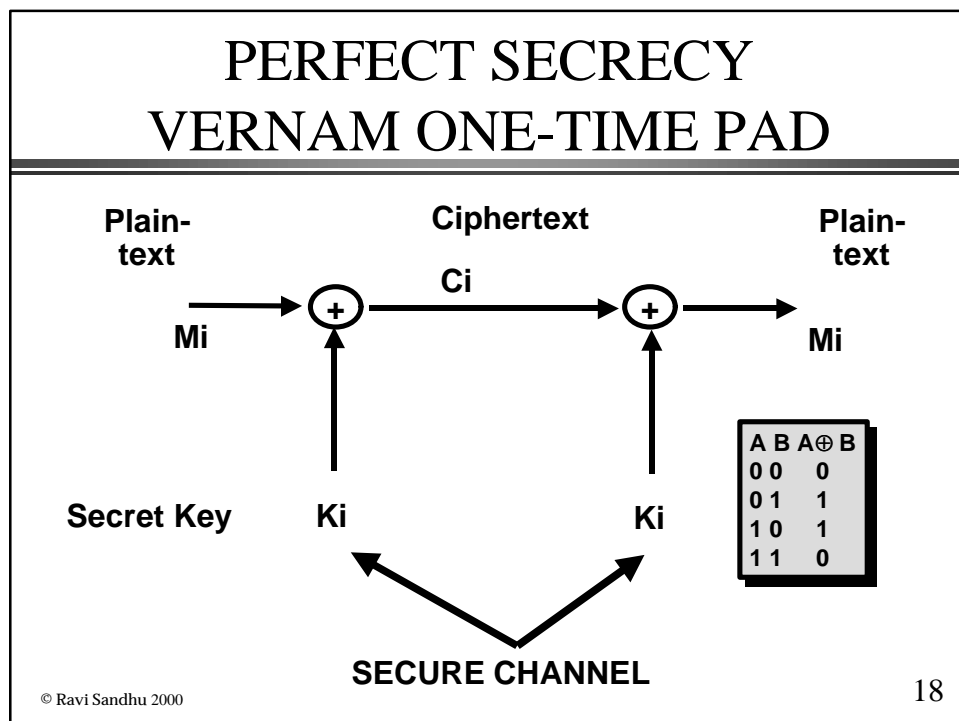
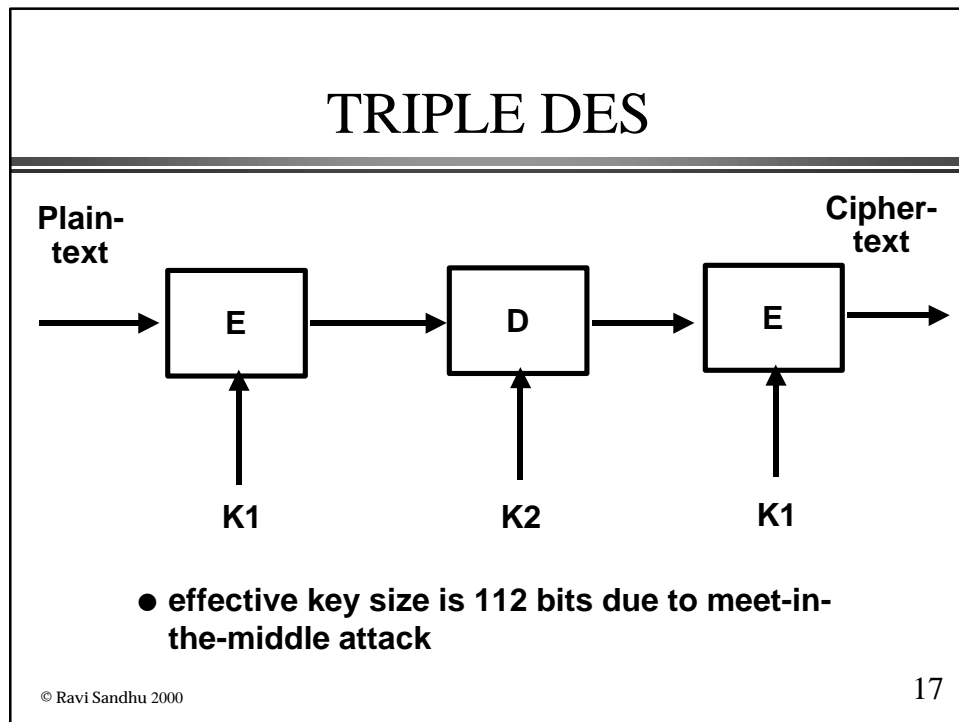


- effective key size is only 57 bits due to meet-in-the-middle attack

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## PERFECT SECRECY VERNAM ONE-TIME PAD

- ◆ **known plaintext reveals the portion of the key that has been used, but does not reveal anything about the future bits of the key**
- ◆ **has been used**
- ◆ **can be approximated**

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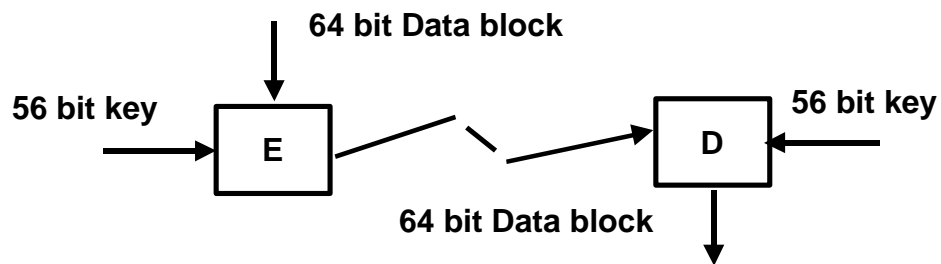
## NEXT GENERATION SECRET KEY CRYPTOSYSTEMS

- ◆ **new Advanced Encryption Standard under development by NIST**
  - **must support key-block combinations of 128-128, 192-128, 256-128**
  - **may support other combinations**
- ◆ **ongoing international competition**
- ◆ **will be in place in a couple of years**

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## ELECTRONIC CODE BOOK (ECB) MODE

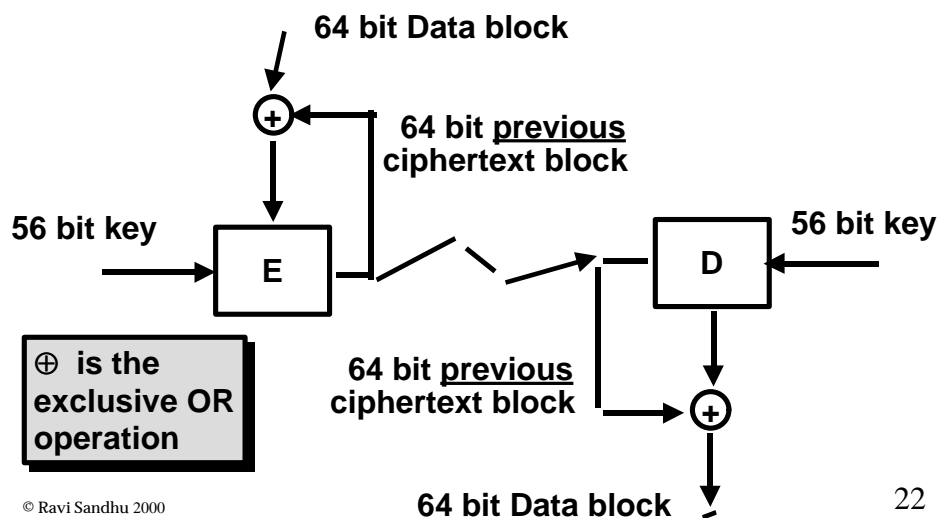


- ♦ OK for small messages
- ♦ identical data blocks will be identically encrypted

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## CIPHER BLOCK CHAINING (CBC) MODE



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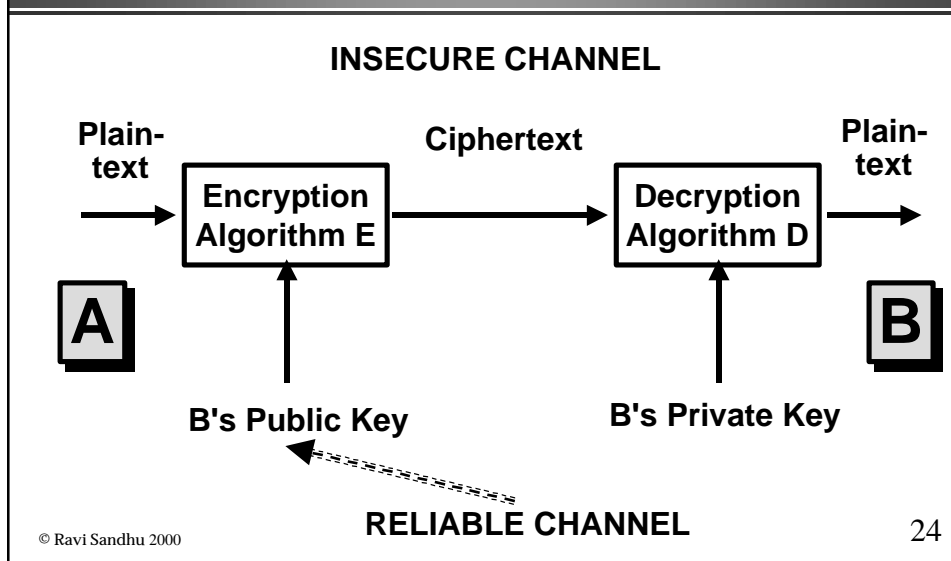
## CIPHER BLOCK CHAINING (CBC) MODE

- ◆ Needs an Initialization Vector (IV) to serve as the first feedback block
- ◆ IV need not be secret or random
- ◆ Integrity of the IV is important, otherwise first data block can be arbitrarily changed.
- ◆ IV should be changed from message to message, or first block of every message should be distinct

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## PUBLIC KEY ENCRYPTION



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## PUBLIC KEY CRYPTOSYSTEM

- ◆ solves the key distribution problem provided there is a reliable channel for communication of public keys
- ◆ requires reliable dissemination of 1 public key/party
- ◆ scales well for large-scale systems

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## PUBLIC KEY ENCRYPTION

- ◆ confidentiality based on infeasibility of computing B's private key from B's public key
- ◆ key sizes are large (512 bits and above) to make this computation infeasible

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## SPEED OF PUBLIC KEY VERSUS SECRET KEY

- ◆ **Public key runs at kilobits/second**
  - think modem connection
- ◆ **Secret key runs at megabits/second and even gigabits/second**
  - think LAN or disk connection
- ◆ **This large difference in speed is likely to remain independent of technology advances**

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## RSA

- ◆ **public key is (n,e)**
- ◆ **private key is d**
- ◆ **encrypt:  $C = M^e \bmod n$**
- ◆ **decrypt:  $M = C^d \bmod n$**

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## GENERATION OF RSA KEYS

- ◆ choose 2 large (100 digit) prime numbers  $p$  and  $q$
- ◆ compute  $n = p * q$
- ◆ pick  $e$  relatively prime to  $(p-1)*(q-1)$
- ◆ compute  $d$ ,  $e*d = 1 \bmod (p-1)*(q-1)$
- ◆ publish  $(n,e)$
- ◆ keep  $d$  secret (and discard  $p, q$ )

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## PROTECTION OF RSA KEYS

- ◆ compute  $d$ ,  $e*d = 1 \bmod (p-1)*(q-1)$ 
  - if factorization of  $n$  into  $p*q$  is known, this is easy to do
- ◆ security of RSA is no better than the difficulty of factoring  $n$  into  $p, q$

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## RSA KEY SIZE

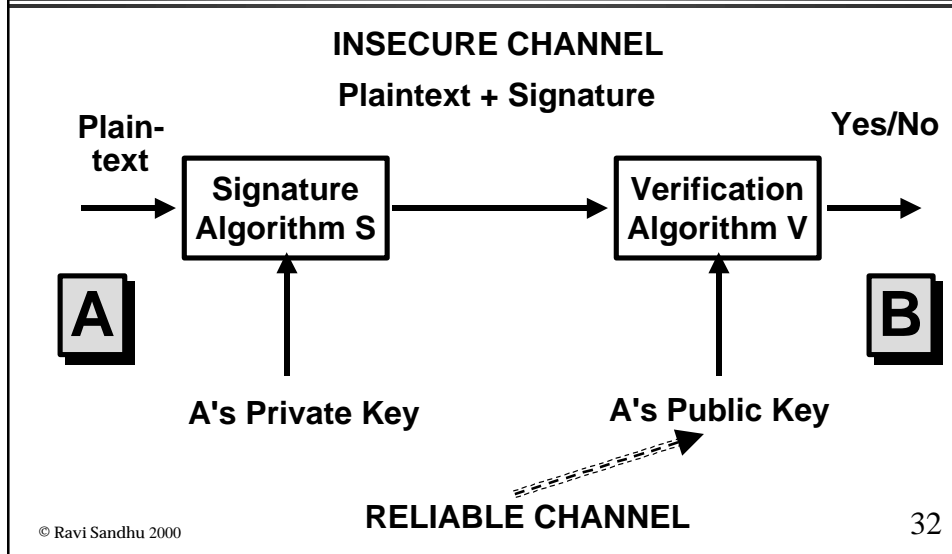
◆ **key size of RSA is selected by the user**

- casual 384 bits
- “commercial” 512 bits
- “military” 1024 bits

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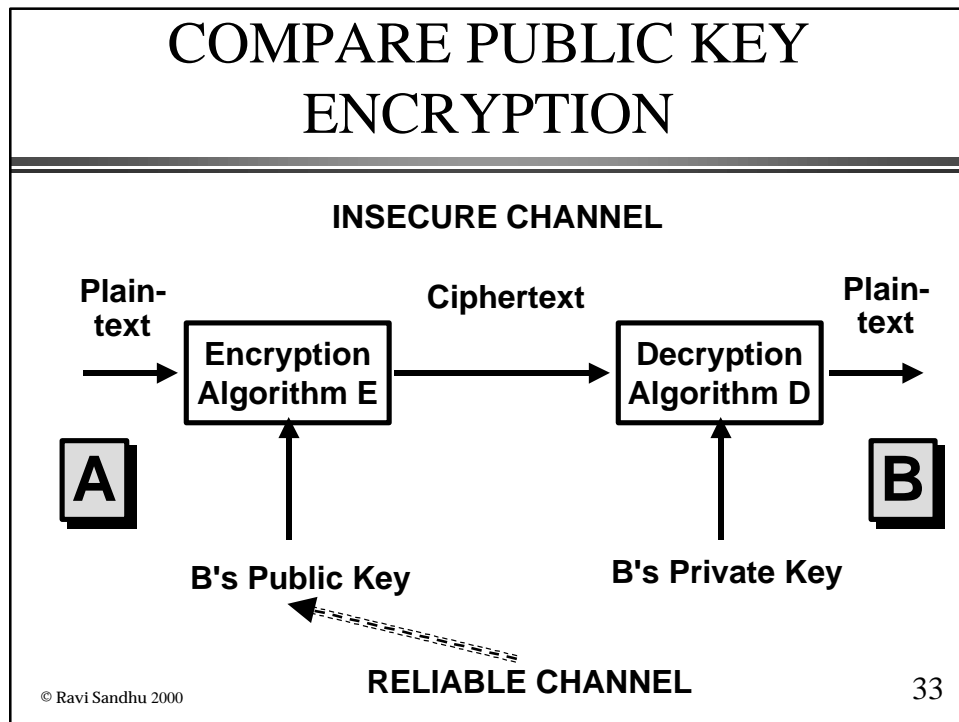
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## DIGITAL SIGNATURES



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## DIGITAL SIGNATURES IN RSA

- ◆ RSA has a unique property, not shared by other public key systems
- ◆ Encryption and decryption commute
  - $(M^e \bmod n)^d \bmod n = M$       encryption
  - $(M^d \bmod n)^e \bmod n = M$       signature
- ◆ Same public key can be use for encryption and signature

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## EL GAMAL AND VARIANTS

- ◆ encryption only
- ◆ signature only
  - 1000's of variants
  - including NIST's DSA

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## NIST DIGITAL SIGNATURE STANDARD

- ◆ System-wide constants
  - $p$  512-1024 bit prime
  - $q$  160 bit prime divisor of  $p-1$
  - $g$   $g = h^{((p-1)/q)} \bmod p$ ,  $1 < h < p-1$
- ◆ El-Gamal variant
  - separate algorithms for digital signature and public-key encryption

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## NIST DIGITAL SIGNATURE STANDARD

- ◆ **to sign message m: private key x**
  - choose random r
  - compute  $v = (g^r \bmod p) \bmod q$
  - compute  $s = (m + xv)/k \bmod q$
  - signature is (s,v,m)
- ◆ **to verify signature: public key y**
  - compute  $u1 = m/s \bmod q$
  - compute  $u2 = v/s \bmod q$
  - verify that  $v = (g^{u1} * y^{u2} \bmod p) \bmod q$

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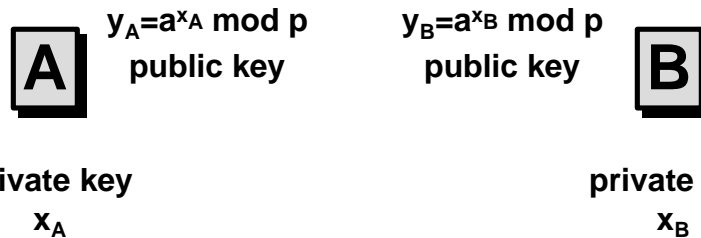
## NIST DIGITAL SIGNATURE STANDARD

- ◆ **signature does not repeat, since r will be different on each occasion**
- ◆ **if same random number r is used for two messages, the system is broken**
- ◆ **message expands by a factor of 2**
- ◆ **RSA signatures do repeat, and there is no message expansion**

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## DIFFIE-HELLMAN KEY ESTABLISHMENT



$$k = y_B^{x_A} \bmod p = y_A^{x_B} \bmod p = a^{x_A \cdot x_B} \bmod p$$

system constants:  $p$ : prime number,  $a$ : integer

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## DIFFIE-HELLMAN KEY ESTABLISHMENT

- ♦ security depends on difficulty of computing  $x$  given  $y = a^x \bmod p$  called the discrete logarithm problem

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## CURRENT GENERATION PUBLIC KEY SYSTEMS

- ◆ **RSA (Rivest, Shamir and Adelman)**
  - the only one to provide digital signature and encryption using the same public-private key pair
  - security based on factoring
- ◆ **ElGamal Encryption**
  - public-key encryption only
  - security based on digital logarithm
- ◆ **DSA signatures**
  - public-key signature only
  - one of many variants of ElGamal signature
  - security based on digital logarithm

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## CURRENT GENERATION PUBLIC KEY SYSTEMS

- ◆ **DH (Diffie-Hellman)**
  - secret key agreement only
  - security based on digital logarithm
- ◆ **ECC (Elliptic curve cryptography)**
  - security based on digital logarithm in elliptic curve field
  - uses analogs of
    - ElGamal encryption
    - DH key agreement
    - DSA digital signature

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## ELLIPTIC CURVE CRYPTOGRAPHY

- ◆ **mathematics is more complicated than RSA or Diffie-Hellman**
- ◆ **elliptic curves have been studied for over one hundred years**
- ◆ **computation is done in a group defined by an elliptic curve**

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## ELLIPTIC CURVE CRYPTOGRAPHY

- ◆ **160 bit ECC public key is claimed to be as secure as 1024 bit RSA or Diffie-Hellman key**
- ◆ **good for small hardware implementations such as smart cards**

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## ELLIPTIC CURVE CRYPTOGRAPHY

- ◆ **ECDSA: Elliptic Curve digital signature algorithm based on NIST Digital Signature Standard**
- ◆ **ECSVA: Elliptic Curve key agreement algorithm based on Diffie-Hellman**
- ◆ **ECES: Elliptic Curve encryption algorithm based on El-Gamal**

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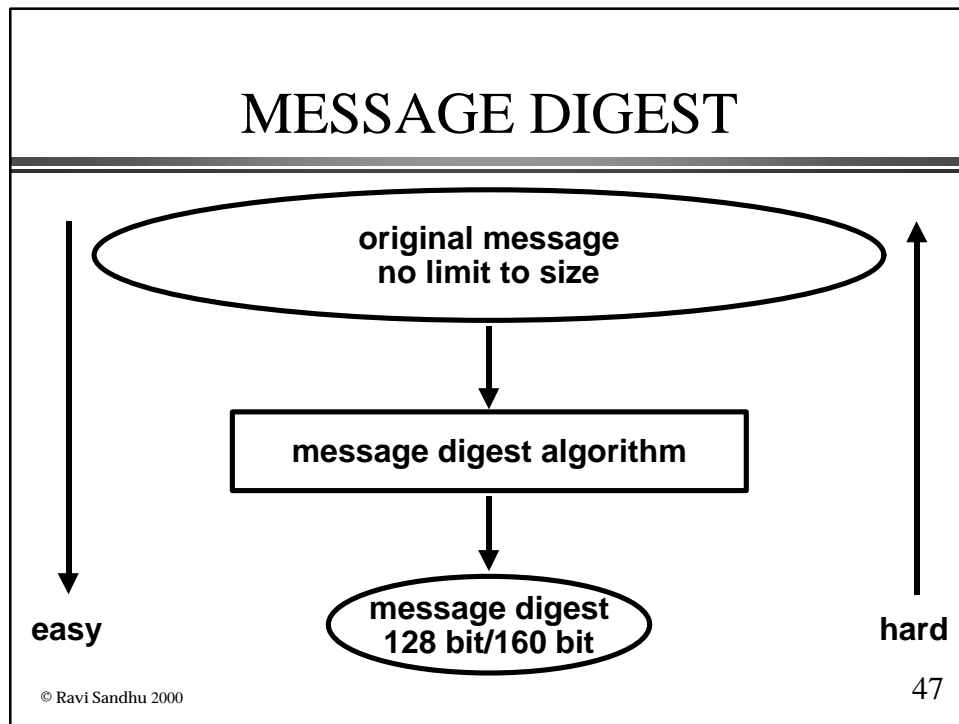
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## PKCS STANDARDS

- ◆ **de facto standards initiated by RSA Data Inc.**

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## MESSAGE DIGEST

- ◆ for performance reasons
  - sign the message digest
  - not the message
- ◆ one way function
  - $m = H(M)$  is easy to compute
  - $M = H^{-1}(m)$  is hard to compute

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## DESIRED CHARACTERISTICS

- ◆ weak hash function
  - difficult to find  $M'$  such that  $H(M')=H(M)$
- ◆ given  $M$ ,  $m=H(M)$  try messages at random to find  $M'$  with  $H(M')=m$ 
  - $2^k$  trials on average,  $k=64$  to be safe

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## DESIRED CHARACTERISTICS

- ◆ strong hash function
  - difficult to find any two  $M$  and  $M'$  such that  $H(M')=H(M)$
- ◆ try pairs of messages at random to find  $M$  and  $M'$  such that  $H(M')=H(M)$ 
  - $2^{k/2}$  trials on average,  $k=128$  to be safe
  - $k=160$  is better

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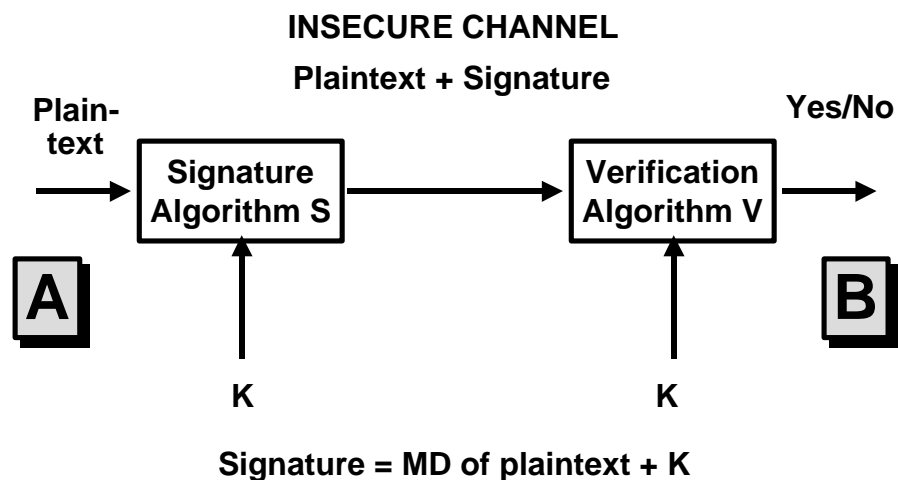
## CURRENTT GENERATION MESSAGE DIGEST ALGORITHMS

- ◆ **MD5 (Message Digest 5)**
  - 128 bit message digest
  - falling out of favor
- ◆ **SHA (Secure Hash Algorithm)**
  - 160 bit message digest
  - slightly slower than MD5 but more secure

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## MESSAGE AUTHENTICATION CODES



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## CURRENT GENERATION MAC ALGORITHMS

- ◆ **HMAC-MD5, HMAC-SHA**
  - IETF standard
  - general technique for constructing a MAC from a message digest algorithm
- ◆ **Older MACs are based on secret key encryption algorithms (notably DES) and are still in use**
  - DES based MACs are 64 bit and not considered strong anymore

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## HMAC

- ◆ **HMAC computation**
- ◆  $\text{HMAC}_K(M) = h(K \oplus \text{opad} \parallel h(K \oplus \text{ipad} \parallel M))$ 
  - $h$  is any message digest function
  - $M$  message
  - $K$  secret key
  - opad, ipad: fixed outer and inner padding
- ◆ **HMAC-MD5, HMAC-SHA**

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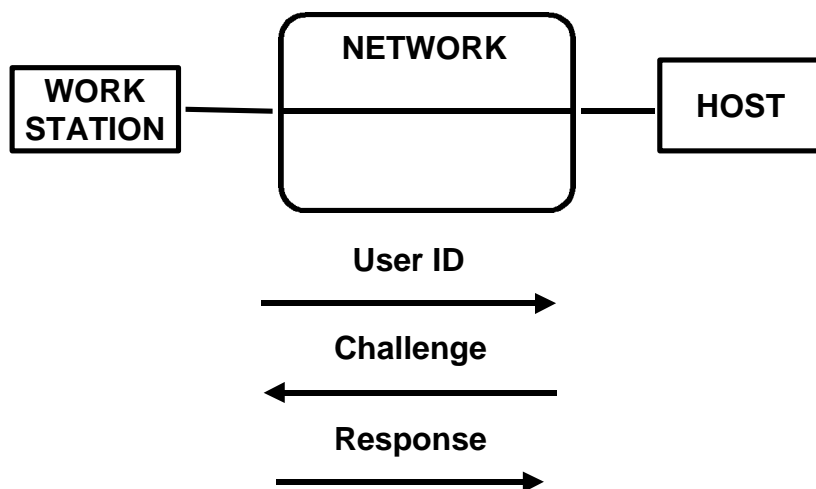
## SAFE CRYPTOGRAPHY

- ◆ **Secret-key encryption**
  - 128 bit or higher
- ◆ **Public-key**
  - 1024 bit or higher
- ◆ **Message digests**
  - 160 bit or higher
- ◆ **A large portion of what is deployed is much weaker**

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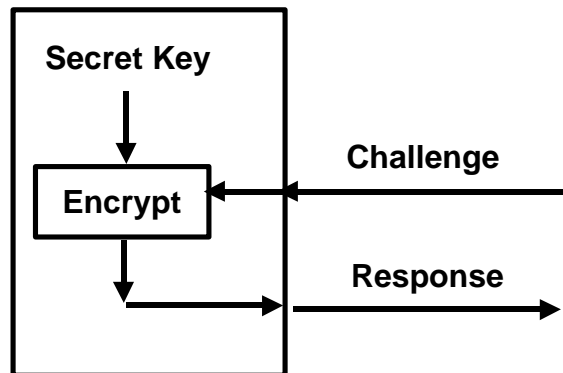
## STRONG AUTHENTICATION CHALLENGE RESPONSE



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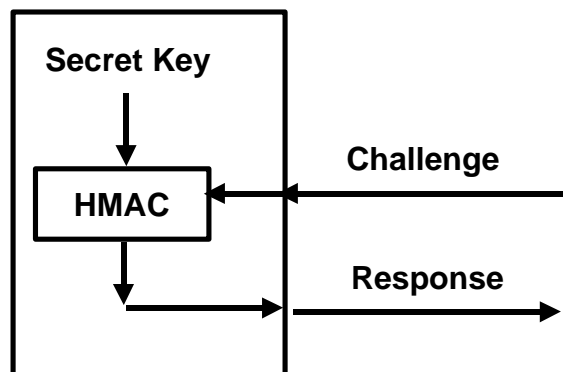
## CHALLENGE RESPONSE



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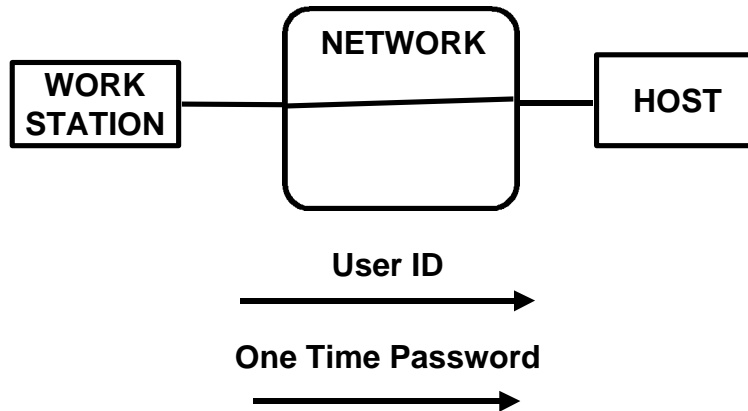
## CHALLENGE RESPONSE



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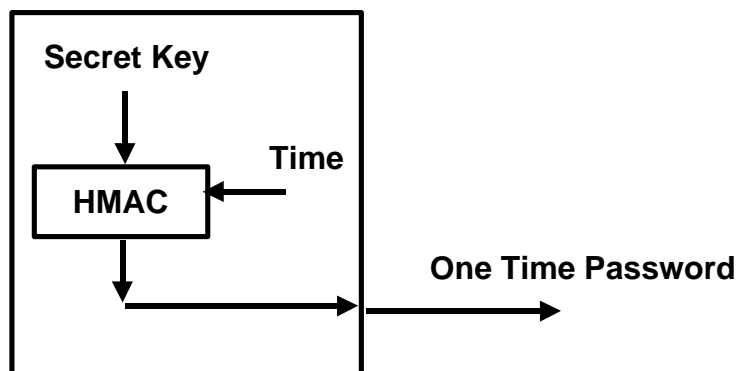
## TIME SYNCHRONIZED



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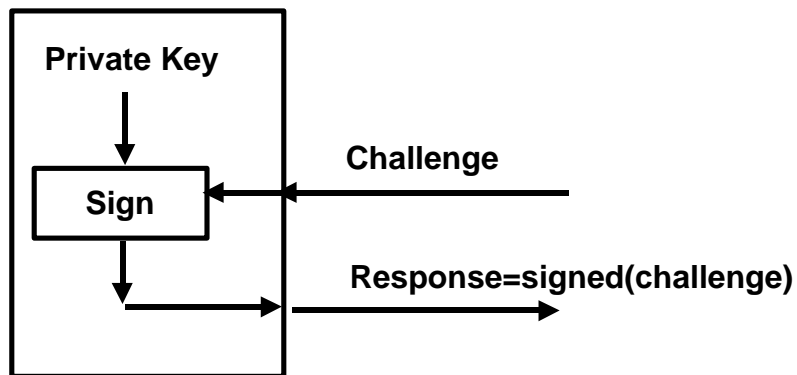
## TIME SYNCHRONIZED



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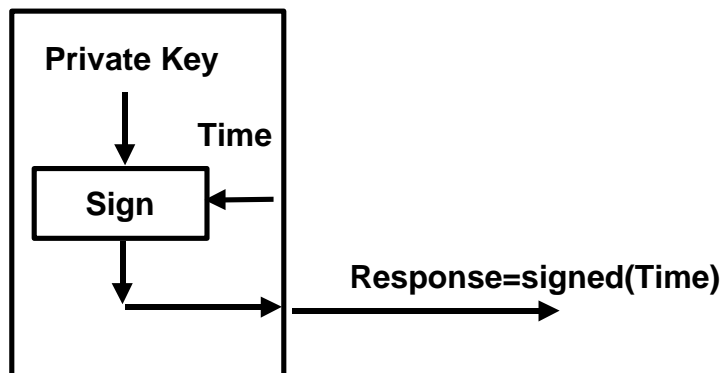
## PUBLIC KEY BASED



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## PUBLIC KEY BASED



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## **PUBLIC-KEY INFRASTRUCTURE**

### **PUBLIC-KEY CERTIFICATES**

---

- ◆ **reliable distribution of public-keys**
- ◆ **public-key encryption**
  - sender needs public key of receiver
- ◆ **public-key digital signatures**
  - receiver needs public key of sender
- ◆ **public-key key agreement**
  - both need each other's public keys



## X.509 CERTIFICATE

VERSION
SERIAL NUMBER
SIGNATURE ALGORITHM
ISSUER
VALIDITY
SUBJECT
SUBJECT PUBLIC KEY INFO
<i>SIGNATURE</i>

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## X.509 CERTIFICATE

1
1234567891011121314
RSA+MD5, 512
C=US, S=VA, O=GMU, OU=ISSE
9/9/99-1/1/1
C=US, S=VA, O=GMU, OU=ISSE, CN=Ravi Sandhu
RSA, 1024, xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx
<i>SIGNATURE</i>

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66

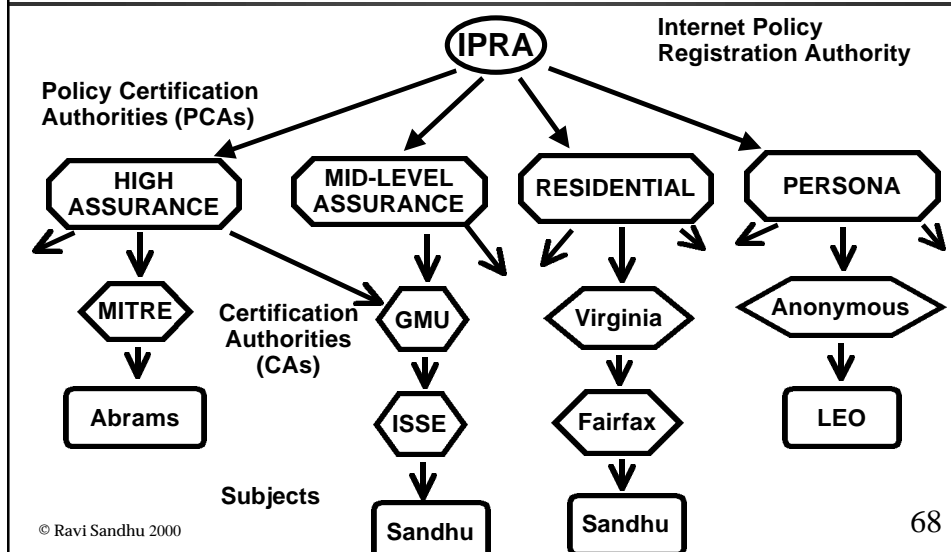
## CERTIFICATE TRUST

- ◆ how to acquire public key of the issuer to verify signature
- ◆ whether or not to trust certificates signed by the issuer for this subject

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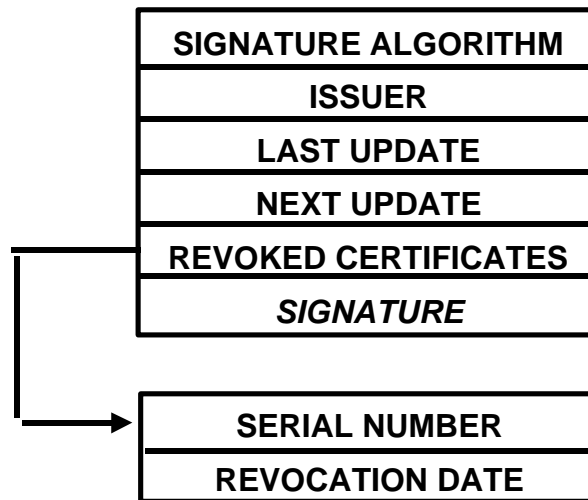
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## PEM CERTIFICATION GRAPH



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## CRL FORMAT



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## X.509 CERTIFICATES

- ◆ **X.509v1**
  - very basic
- ◆ **X.509v2**
  - adds unique identifiers to prevent against reuse of X.500 names
- ◆ **X.509v3**
  - adds many extensions
  - can be further extended

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## X.509v3 CERTIFICATE INNOVATIONS

- ◆ **distinguish various certificates**
  - signature, encryption, key-agreement
- ◆ **identification info in addition to X.500 name**
  - internet names: email addresses, host names, URLs
- ◆ **issuer can state policy and usage**
  - good enough for casual email but not for signing checks
- ◆ **limits on use of signature keys for further certification**
- ◆ **extensible**
  - proprietary extensions can be defined and registered
- ◆ **attribute certificates**
  - ongoing work

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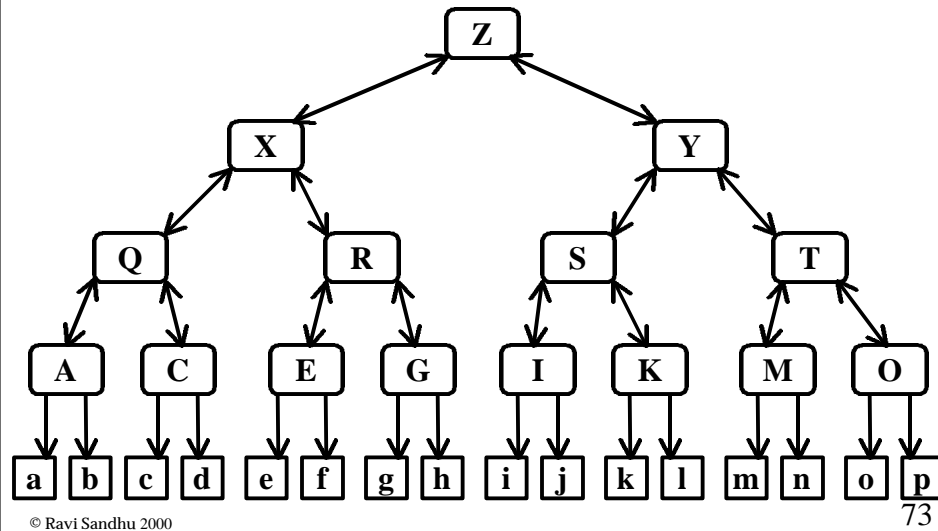
## X.509v2 CRL INNOVATIONS

- ◆ **CRL distribution points**
- ◆ **indirect CRLs**
- ◆ **delta CRLs**
- ◆ **revocation reason**
- ◆ **push CRLs**

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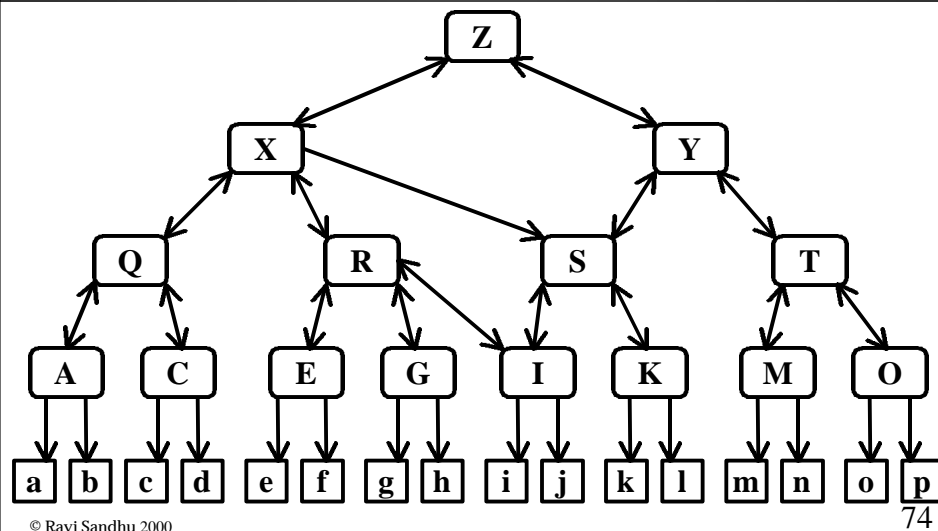
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## GENERAL HIERARCHICAL STRUCTURE



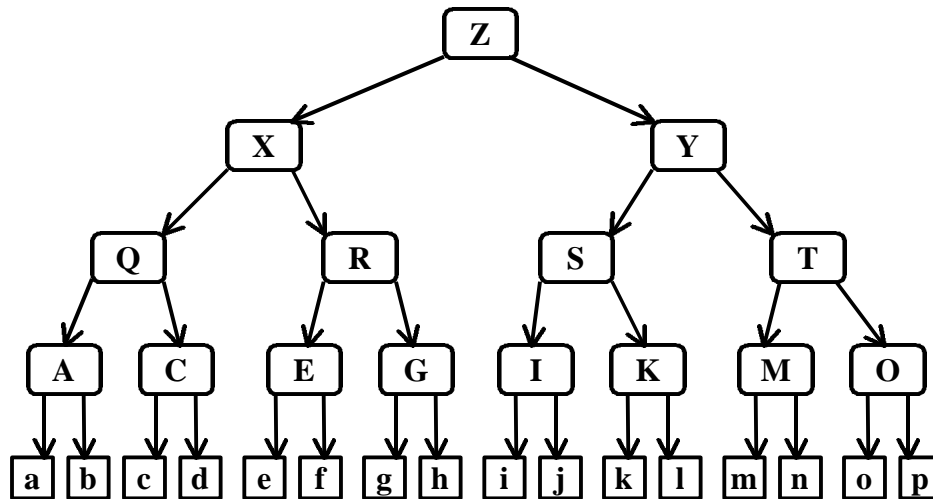
73

## GENERAL HIERARCHICAL STRUCTURE WITH ADDED LINKS



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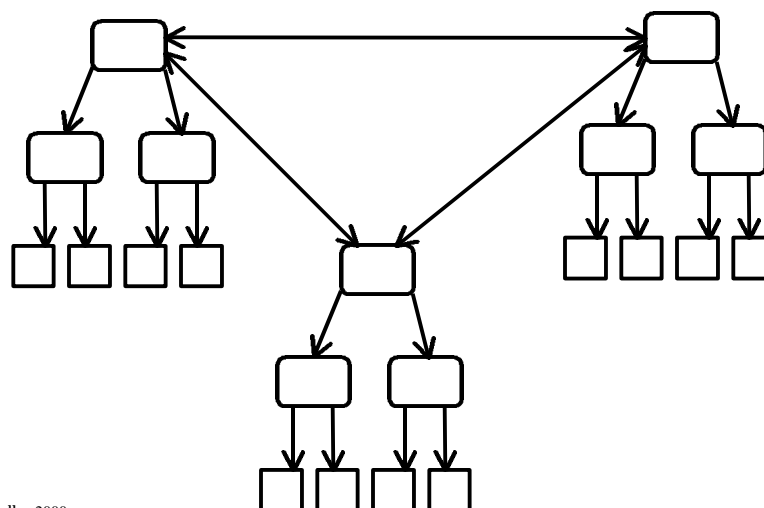
# TOP-DOWN HIERARCHICAL STRUCTURE



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# FOREST OF HIERARCHIES



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