

**INFS 766**  
**Internet Security Protocols**

**Lectures 3 and 4**  
**Cryptography in network protocols**

**Prof. Ravi Sandhu**

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**CRYPTOGRAPHY**

# CRYPTOGRAPHIC TECHNOLOGY



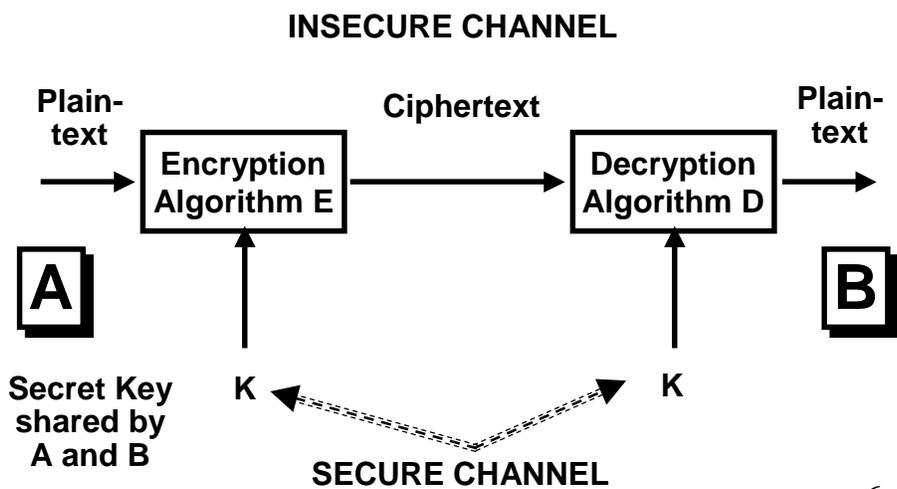
# CRYPTOGRAPHIC TECHNOLOGY

- ❖ **Secret-key encryption**
- ❖ **Public-key encryption**
- ❖ **Public-key digital signatures**
- ❖ **Public-key key agreement**
- ❖ **Message digests**
- ❖ **Message authentication codes**
- ❖ **Challenge-response authentication**
- ❖ **Public-key certificates**

# CRYPTOGRAPHIC SERVICES

- ❖ confidentiality
  - traffic flow confidentiality
- ❖ integrity
- ❖ authentication
- ❖ non-repudiation

# SECRET KEY CRYPTOSYSTEM



## SECRET KEY CRYPTOSYSTEM

- ❖ **confidentiality depends only on secrecy of the key**
  - size of key is critical
- ❖ **secret key systems do not scale well**
  - with  $N$  parties we need to generate and distribute  $N*(N-1)/2$  keys
- ❖ **A and B can be people or computers**

## MASTER KEYS AND SESSION KEYS

- ❖ **long-term or master keys**
  - prolonged use increases exposure
- ❖ **session keys**
  - short-term keys communicated by means of
    - long-term secret keys
    - public key technology

# CRYPTANALYSIS

- ❖ **ciphertext only**
  - cryptanalyst only knows ciphertext
- ❖ **known plaintext**
  - cryptanalyst knows some plaintext-ciphertext pairs
- ❖ **chosen plaintext**
- ❖ **chosen ciphertext**

# KNOWN PLAINTEXT ATTACK

- ❖ **40 bit key requires  $2^{39} \approx 5 * 10^{11}$  trials on average (exportable from USA)**
- ❖ **trials/second time required**

<b>1</b>	<b>20,000 years</b>
<b><math>10^3</math></b>	<b>20 years</b>
<b><math>10^6</math></b>	<b>6 days</b>
<b><math>10^9</math></b>	<b>9 minutes</b>
<b><math>10^{12}</math></b>	<b>0.5 seconds</b>

## KNOWN PLAINTEXT ATTACK

❖ 56 bit key requires  $2^{55} \approx 3.6 * 10^{16}$  trials on average (DES)

❖ trials/second time required

1	$10^9$ years
$10^3$	$10^6$ years
$10^6$	$10^3$ years
$10^9$	1 year
$10^{12}$	10 hours

## KNOWN PLAINTEXT ATTACK

❖ 80 bit key requires  $2^{79} \approx 6 * 10^{23}$  trials on average (SKIPJACK)

❖ trials/second time required

1	$10^{16}$ years
$10^3$	$10^{13}$ years
$10^6$	$10^{10}$ years
$10^9$	$10^7$ years
$10^{12}$	$10^4$ years

## KNOWN PLAINTEXT ATTACK

❖ **128 bit key requires  $2^{127} \approx 2 * 10^{38}$  trials on average (IDEA)**

❖ **trials/second time required**

<b>1</b>	<b><math>10^{30}</math> years</b>
<b><math>10^3</math></b>	<b><math>10^{27}</math> years</b>
<b><math>10^6</math></b>	<b><math>10^{24}</math> years</b>
<b><math>10^9</math></b>	<b><math>10^{21}</math> years</b>
<b><math>10^{12}</math></b>	<b><math>10^{18}</math> years</b>

## DICTIONARY ATTACKS

❖ **if keys are poorly chosen known plaintext attacks can be very simple**

❖ **often the user's password is the key**

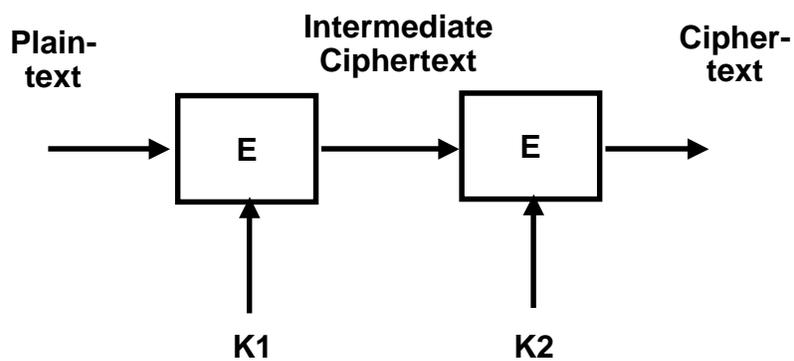
- **in a dictionary attack the cryptanalyst tries passwords from a dictionary, rather than all possible keys**
- **for a 20,000 word dictionary, 1 trial/second will crack a poor password in less than 3 hours**

## CURRENT GENERATION SECRET KEY CRYPTOSYSTEMS

### ❖ 64 bit data block size

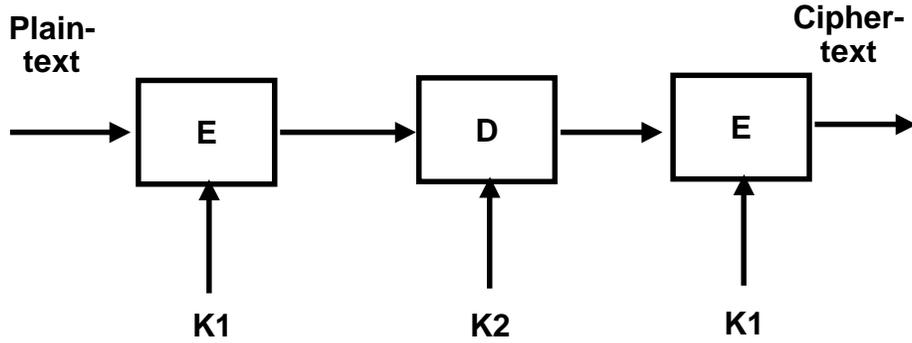
- DES: 56 bit key
- Triple DES: 112 bit key
- Triple DES: 168 bit key
- Skipjack: 80 bit key
- IDEA: 128 bit key
- RC2: variable size key: 1 byte to 128 bytes
- many others

## DOUBLE DES



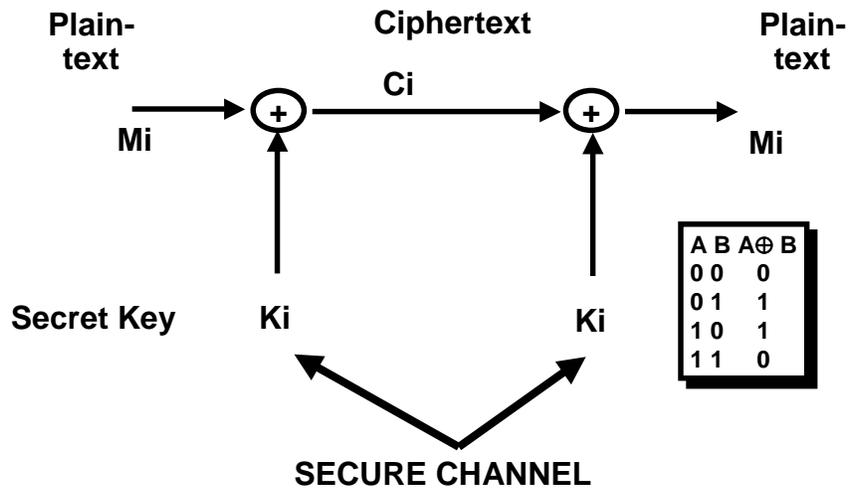
- effective key size is only 57 bits due to meet-in-the-middle attack

# TRIPLE DES



➤ effective key size is 112 bits due to meet-in-the-middle attack

# PERFECT SECRECY VERNAM ONE-TIME PAD



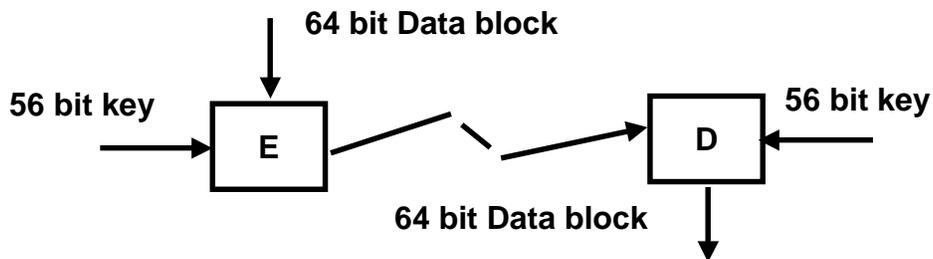
## PERFECT SECRECY VERNAM ONE-TIME PAD

- ❖ **known plaintext reveals the portion of the key that has been used, but does not reveal anything about the future bits of the key**
- ❖ **has been used**
- ❖ **can be approximated**

## ADVANCED ENCRYPTION STANDARD

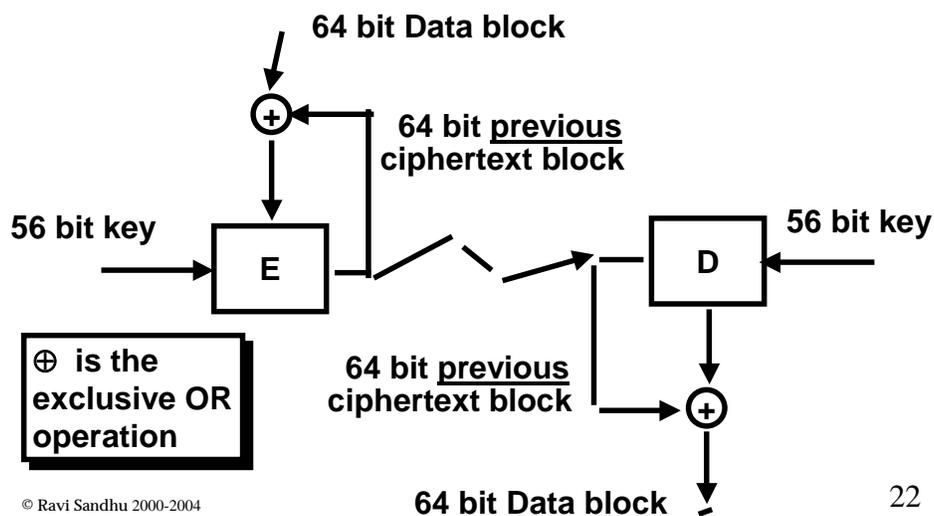
- ❖ **New Advanced Encryption Standard under development by NIST**
  - **must support key-block combinations of 128-128, 192-128, 256-128**
  - **may support other combinations**
- ❖ **selection of Rijndael algorithm announced in 2000**
- ❖ **will be in place in a couple of years**

# ELECTRONIC CODE BOOK (ECB) MODE



- ❖ OK for small messages
- ❖ identical data blocks will be identically encrypted

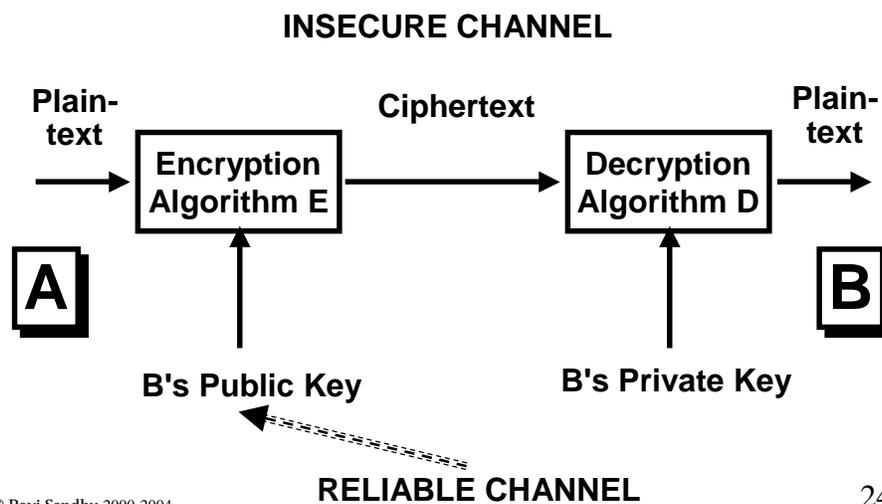
# CIPHER BLOCK CHAINING (CBC) MODE



## CIPHER BLOCK CHAINING (CBC) MODE

- ❖ Needs an Initialization Vector (IV) to serve as the first feedback block
- ❖ IV need not be secret or random
- ❖ Integrity of the IV is important, otherwise first data block can be arbitrarily changed.
- ❖ IV should be changed from message to message, or first block of every message should be distinct

## PUBLIC KEY ENCRYPTION



## PUBLIC KEY CRYPTOSYSTEM

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- ❖ **solves the key distribution problem provided there is a reliable channel for communication of public keys**
- ❖ **requires reliable dissemination of 1 public key/party**
- ❖ **scales well for large-scale systems**

## PUBLIC KEY ENCRYPTION

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- ❖ **confidentiality based on infeasibility of computing B's private key from B's public key**
- ❖ **key sizes are large (512 bits and above) to make this computation infeasible**

## SPEED OF PUBLIC KEY VERSUS SECRET KEY

- ❖ **Public key runs at kilobits/second**
  - think modem connection
- ❖ **Secret key runs at megabits/second and even gigabits/second**
  - think LAN or disk connection
- ❖ **This large difference in speed is likely to remain independent of technology advances**

## RSA

- ❖ **public key is (n,e)**
- ❖ **private key is d**
- ❖ **encrypt:  $C = M^e \text{ mod } n$**
- ❖ **decrypt:  $M = C^d \text{ mod } n$**

## GENERATION OF RSA KEYS

- ❖ choose 2 large (100 digit) prime numbers  $p$  and  $q$
- ❖ compute  $n = p * q$
- ❖ pick  $e$  relatively prime to  $(p-1)*(q-1)$
- ❖ compute  $d$ ,  $e*d = 1 \text{ mod } (p-1)*(q-1)$
- ❖ publish  $(n,e)$
- ❖ keep  $d$  secret (and discard  $p, q$ )

## PROTECTION OF RSA KEYS

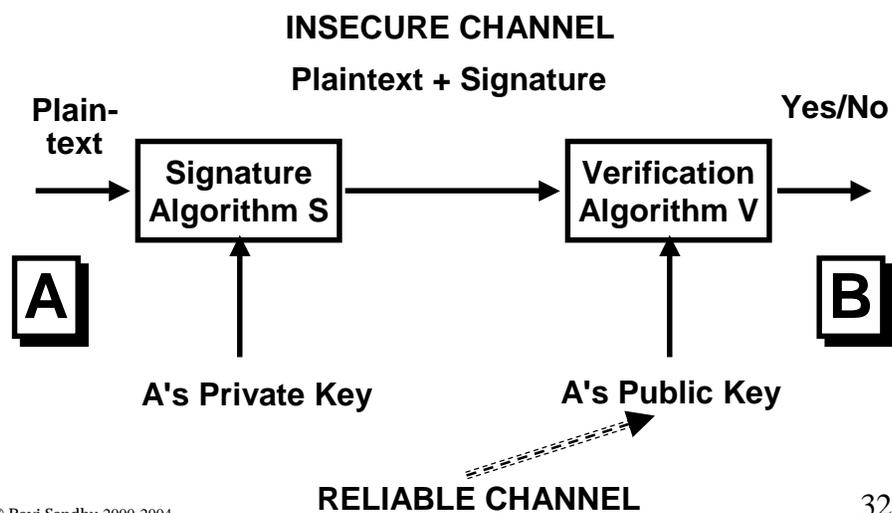
- ❖ compute  $d$ ,  $e*d = 1 \text{ mod } (p-1)*(q-1)$ 
  - if factorization of  $n$  into  $p*q$  is known, this is easy to do
- ❖ security of RSA is no better than the difficulty of factoring  $n$  into  $p, q$

## RSA KEY SIZE

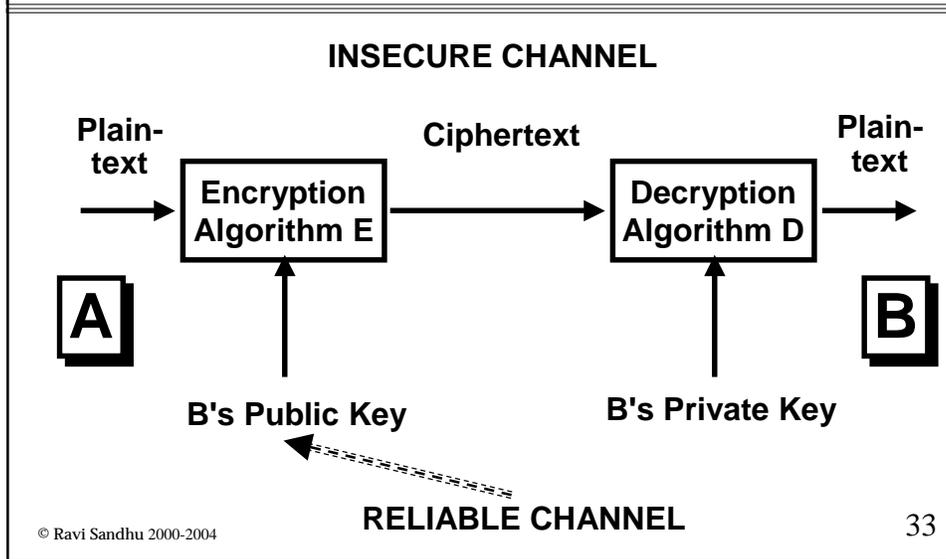
❖ **key size of RSA is selected by the user**

- **casual**                    **384 bits**
- **“commercial”**        **512 bits**
- **“military”**            **1024 bits**

## DIGITAL SIGNATURES



# COMPARE PUBLIC KEY ENCRYPTION



# DIGITAL SIGNATURES IN RSA

- ❖ **RSA has a unique property, not shared by other public key systems**
- ❖ **Encryption and decryption commute**
  - $(M^e \bmod n)^d \bmod n = M$       encryption
  - $(M^d \bmod n)^e \bmod n = M$       signature
- ❖ **Same public key can be use for encryption and signature**

## EL GAMAL AND VARIANTS

- ❖ **encryption only**
- ❖ **signature only**
  - **1000's of variants**
  - **including NIST's DSA**

## NIST DIGITAL SIGNATURE STANDARD

- ❖ **System-wide constants**
  - **p**      **512-1024 bit prime**
  - **q**      **160 bit prime divisor of p-1**
  - **g**       **$g = h^{((p-1)/q)} \bmod p, 1 < h < p-1$**
- ❖ **El-Gamal variant**
  - **separate algorithms for digital signature and public-key encryption**

## NIST DIGITAL SIGNATURE STANDARD

- ❖ **to sign message m: private key x**
  - choose random r
  - compute  $v = (g^r \bmod p) \bmod q$
  - compute  $s = (m+xv)/k \bmod q$
  - signature is (s,v,m)
- ❖ **to verify signature: public key y**
  - compute  $u1 = m/s \bmod q$
  - compute  $u2 = v/s \bmod q$
  - verify that  $v = (g^{u1} * y^{u2} \bmod p) \bmod q$

## NIST DIGITAL SIGNATURE STANDARD

- ❖ **signature does not repeat, since r will be different on each occasion**
- ❖ **if same random number r is used for two messages, the system is broken**
- ❖ **message expands by a factor of 2**
- ❖ **RSA signatures do repeat, and there is no message expansion**

# DIFFIE-HELLMAN KEY AGREEMENT

$$\boxed{\mathbf{A}} \quad y_A = a^{x_A} \bmod p \quad \text{public key} \quad y_B = a^{x_B} \bmod p \quad \text{public key} \quad \boxed{\mathbf{B}}$$

private key  
 $x_A$

private key  
 $x_B$

$$k = y_B^{x_A} \bmod p = y_A^{x_B} \bmod p = a^{x_A x_B} \bmod p$$

system constants:  $p$ : prime number,  $a$ : integer

# DIFFIE-HELLMAN KEY ESTABLISHMENT

❖ security depends on difficulty of computing  $x$  given  $y = a^x \bmod p$  called the discrete logarithm problem

# MAN IN THE MIDDLE ATTACK

**A**

**C**

**B**

# CURRENT GENERATION PUBLIC KEY SYSTEMS

- ❖ **RSA (Rivest, Shamir and Adelman)**
  - the only one to provide digital signature and encryption using the same public-private key pair
  - security based on factoring
- ❖ **EIGamal Encryption**
  - public-key encryption only
  - security based on digital logarithm
- ❖ **DSA signatures**
  - public-key signature only
  - one of many variants of EIGamal signature
  - security based on digital logarithm

# CURRENT GENERATION PUBLIC KEY SYSTEMS

- ❖ **DH (Diffie-Hellman)**
  - secret key agreement only
  - security based on digital logarithm
- ❖ **ECC (Elliptic curve cryptography)**
  - security based on digital logarithm in elliptic curve field
  - uses analogs of
    - ElGamal encryption
    - DH key agreement
    - DSA digital signature

# ELLIPTIC CURVE CRYPTOGRAPHY

- ❖ **mathematics is more complicated than RSA or Diffie-Hellman**
- ❖ **elliptic curves have been studied for over one hundred years**
- ❖ **computation is done in a group defined by an elliptic curve**

## ELLIPTIC CURVE CRYPTOGRAPHY

- ❖ **160 bit ECC public key is claimed to be as secure as 1024 bit RSA or Diffie-Hellman key**
- ❖ **good for small hardware implementations such as smart cards**

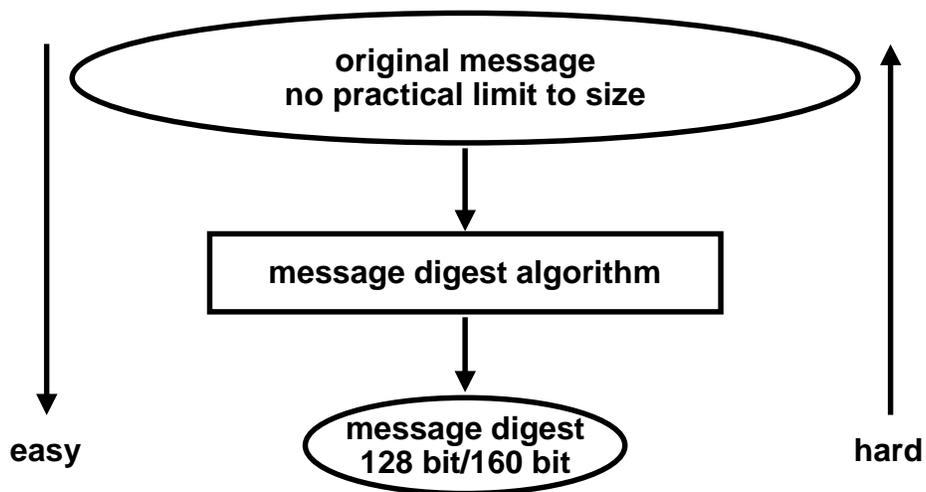
## ELLIPTIC CURVE CRYPTOGRAPHY

- ❖ **ECDSA: Elliptic Curve digital signature algorithm based on NIST Digital Signature Standard**
- ❖ **ECSVA: Elliptic Curve key agreement algorithm based on Diffie-Hellman**
- ❖ **ECES: Elliptic Curve encryption algorithm based on El-Gamal**

# PKCS STANDARDS

❖ **de facto standards initiated by RSA Data Inc.**

# MESSAGE DIGEST



## MESSAGE DIGEST

- ❖ **for performance reasons**
  - sign the message digest
  - not the message
- ❖ **one way function**
  - $m=H(M)$  is easy to compute
  - $M=H^{-1}(m)$  is hard to compute

## DESIRED CHARACTERISTICS

- ❖ **weak hash function**
  - difficult to find  $M'$  such that  $H(M')=H(M)$
- ❖ **given  $M$ ,  $m=H(M)$  try messages at random to find  $M'$  with  $H(M')=m$** 
  - $2^k$  trials on average,  $k=64$  to be safe

## DESIRED CHARACTERISTICS

### ❖ strong hash function

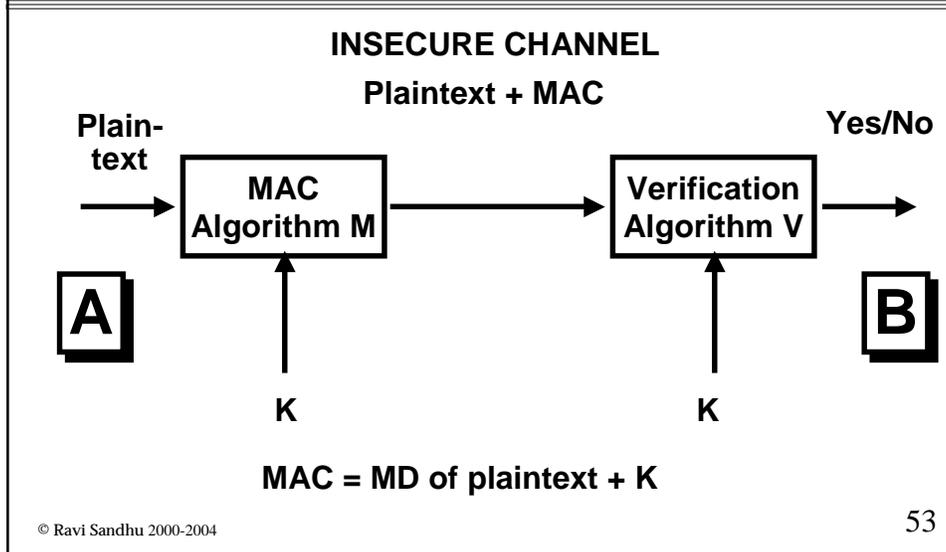
- difficult to find any two  $M$  and  $M'$  such that  $H(M')=H(M)$
- ❖ try pairs of messages at random to find  $M$  and  $M'$  such that  $H(M')=H(M)$ 
  - $2^{k/2}$  trials on average,  $k=128$  to be safe
  - $k=160$  is better

## CURRENTT GENERATION MESSAGE DIGEST ALGORITHMS

### ❖ MD5 (Message Digest 5)

- 128 bit message digest
- falling out of favor
- ❖ SHA (Secure Hash Algorithm)
  - 160 bit message digest
  - slightly slower than MD5 but more secure

# MESSAGE AUTHENTICATION CODES



# CURRENT GENERATION MAC ALGORITHMS

- ❖ **HMAC-MD5, HMAC-SHA**
  - IETF standard
  - general technique for constructing a MAC from a message digest algorithm
- ❖ **Older MACs are based on secret key encryption algorithms (notably DES) and are still in use**
  - DES based MACs are 64 bit and not considered strong anymore

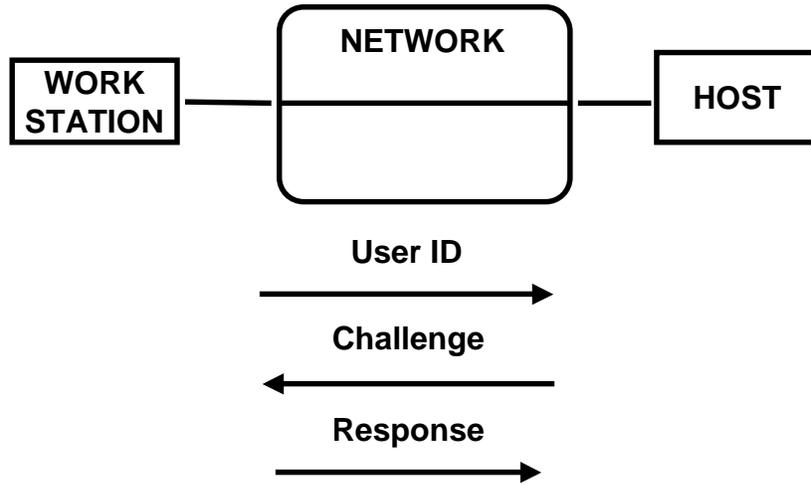
# HMAC

- ❖ **HMAC computation**
- ❖  $\text{HMAC}_K(M) = h(K \oplus \text{opad} || h(K \oplus \text{ipad} || M))$ 
  - **h** is any message digest function
  - **M** message
  - **K** secret key
  - **opad, ipad**: fixed outer and inner padding
- ❖ **HMAC-MD5, HMAC-SHA**

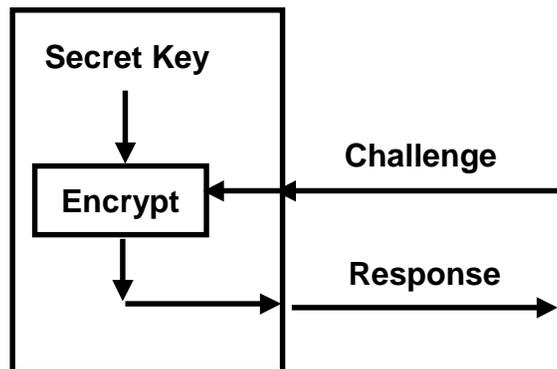
# SAFE CRYPTOGRAPHY

- ❖ **Secret-key encryption**
  - 128 bit or higher
- ❖ **Public-key**
  - 1024 bit or higher
- ❖ **Message digests**
  - 160 bit or higher
- ❖ **A large portion of what is deployed is much weaker**

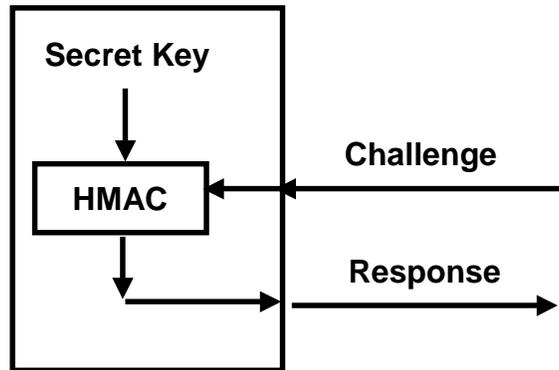
# STRONG AUTHENTICATION CHALLENGE RESPONSE



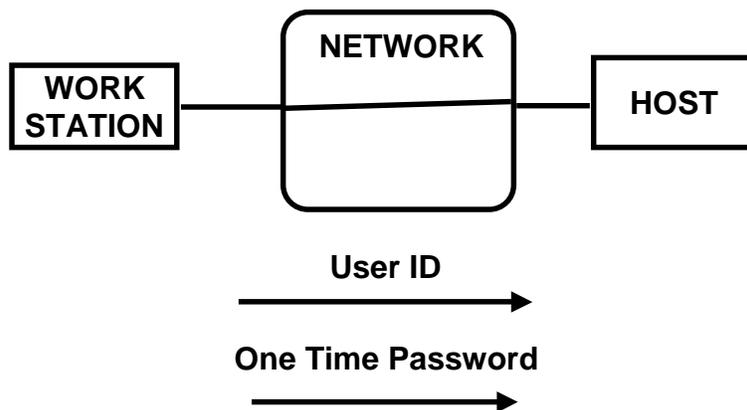
# CHALLENGE RESPONSE



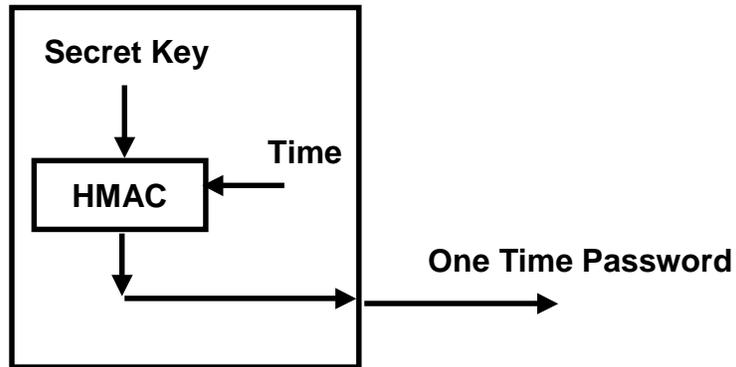
# CHALLENGE RESPONSE



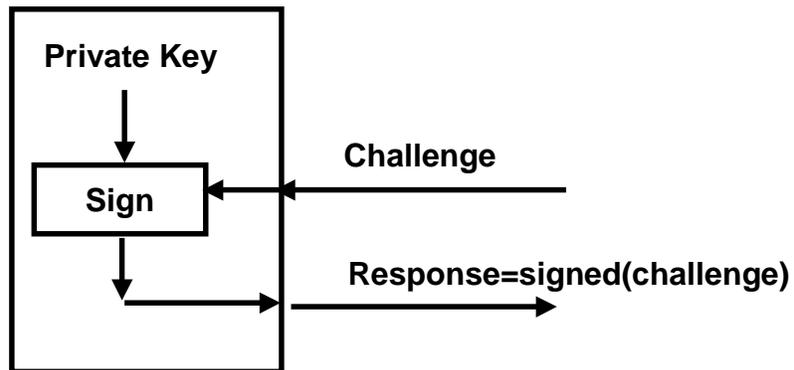
# TIME SYNCHRONIZED



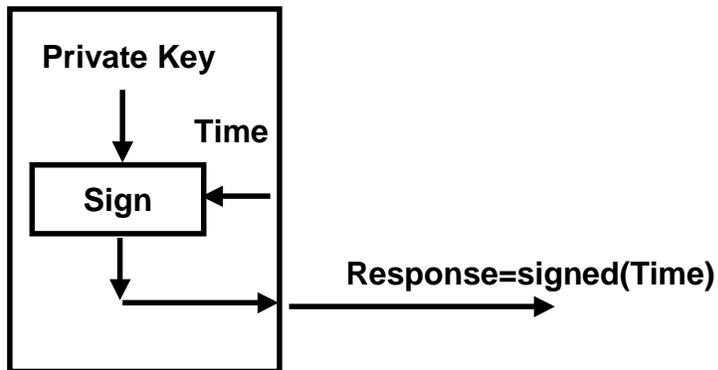
# TIME SYNCHRONIZED



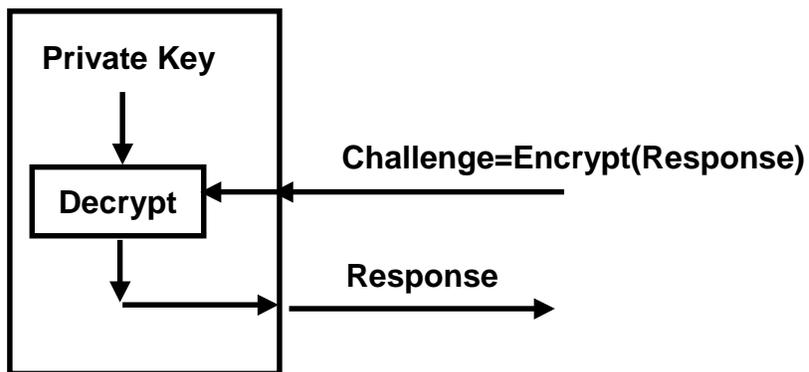
# PUBLIC KEY SIGNATURE BASED



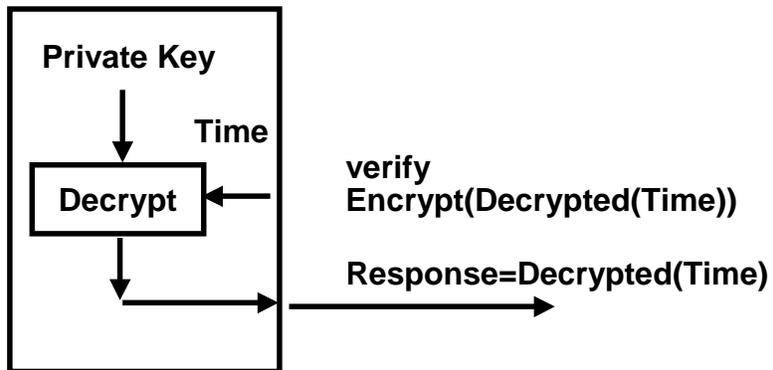
# PUBLIC KEY SIGNATURE BASED



# PUBLIC KEY ENCRYPTION BASED



# PUBLIC KEY ENCRYPT BASED



# PUBLIC-KEY INFRASTRUCTURE

## PUBLIC-KEY CERTIFICATES

- ❖ **reliable distribution of public-keys**
- ❖ **public-key encryption**
  - sender needs public key of receiver
- ❖ **public-key digital signatures**
  - receiver needs public key of sender
- ❖ **public-key key agreement**
  - both need each other's public keys

## X.509v1 CERTIFICATE

<b>VERSION</b>
<b>SERIAL NUMBER</b>
<b>SIGNATURE ALGORITHM</b>
<b>ISSUER</b>
<b>VALIDITY</b>
<b>SUBJECT</b>
<b>SUBJECT PUBLIC KEY INFO</b>
<b><i>SIGNATURE</i></b>

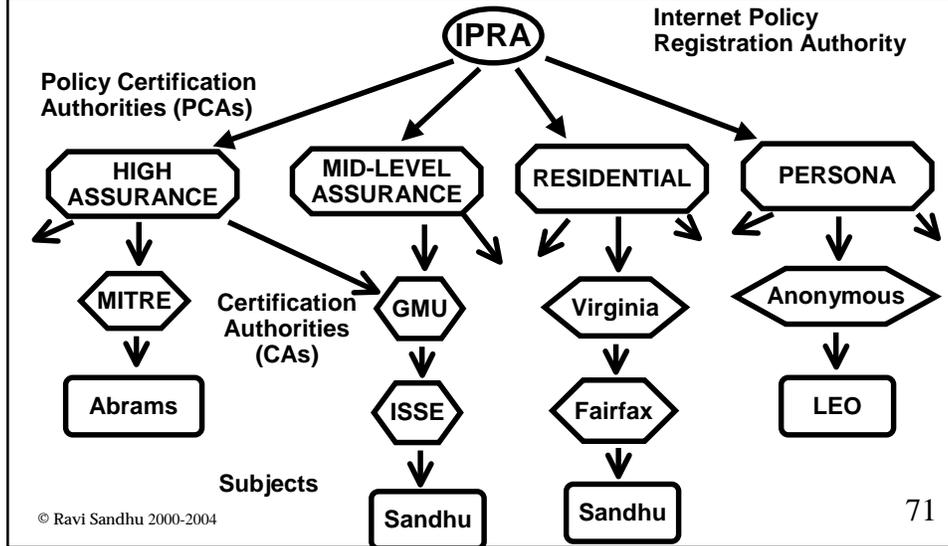
## X.509v1 CERTIFICATE

1
1234567891011121314
RSA+MD5, 512
C=US, S=VA, O=GMU, OU=ISE
9/9/99-1/1/1
C=US, S=VA, O=GMU, OU=ISE, CN=Ravi Sandhu
RSA, 1024, xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx
<i>SIGNATURE</i>

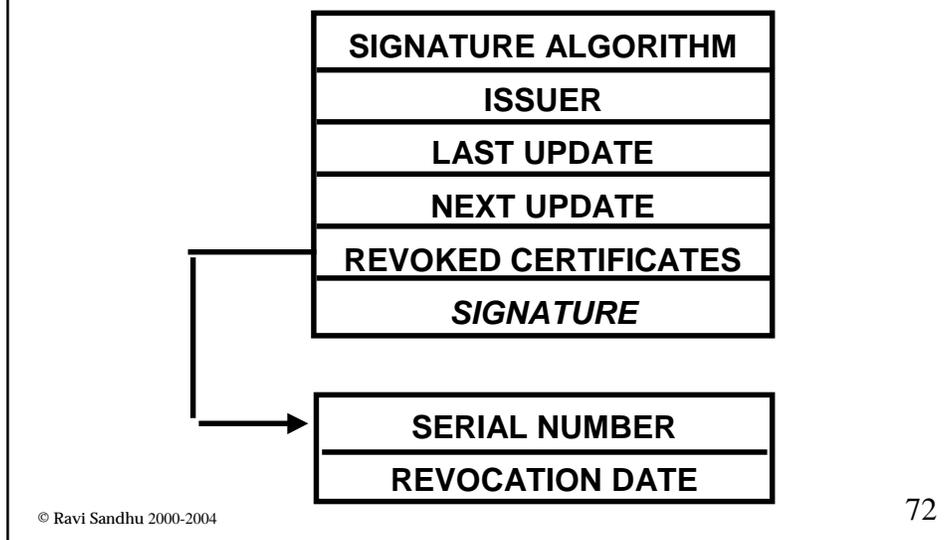
## CERTIFICATE TRUST

- ❖ how to acquire public key of the issuer to verify signature
- ❖ whether or not to trust certificates signed by the issuer for this subject

# PEM CERTIFICATION GRAPH



# CRL FORMAT



## X.509 CERTIFICATES

- ❖ **X.509v1**
  - very basic
- ❖ **X.509v2**
  - adds unique identifiers to prevent against reuse of X.500 names
- ❖ **X.509v3**
  - adds many extensions
  - can be further extended

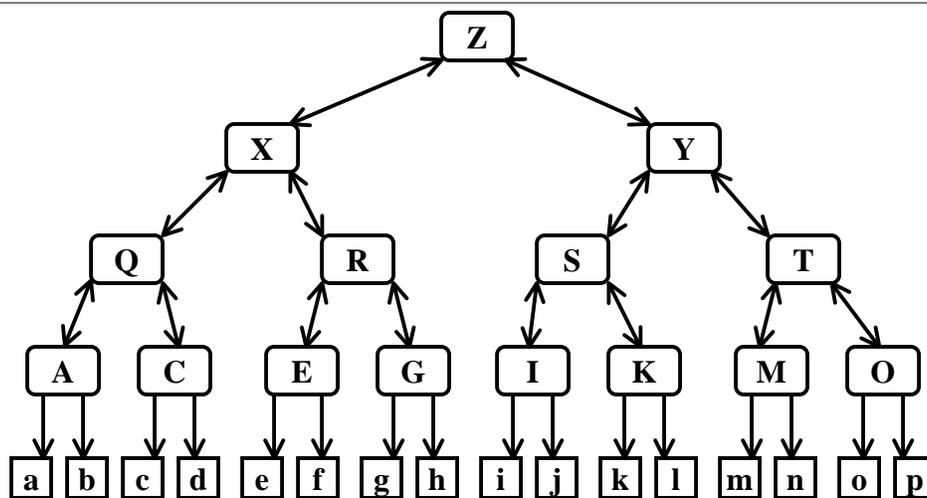
## X.509v3 CERTIFICATE INNOVATIONS

- ❖ **distinguish various certificates**
  - signature, encryption, key-agreement
- ❖ **identification info in addition to X.500 name**
  - internet names: email addresses, host names, URLs
- ❖ **issuer can state policy and usage**
  - good enough for casual email but not for signing checks
- ❖ **limits on use of signature keys for further certification**
- ❖ **extensible**
  - proprietary extensions can be defined and registered
- ❖ **attribute certificates**
  - ongoing work

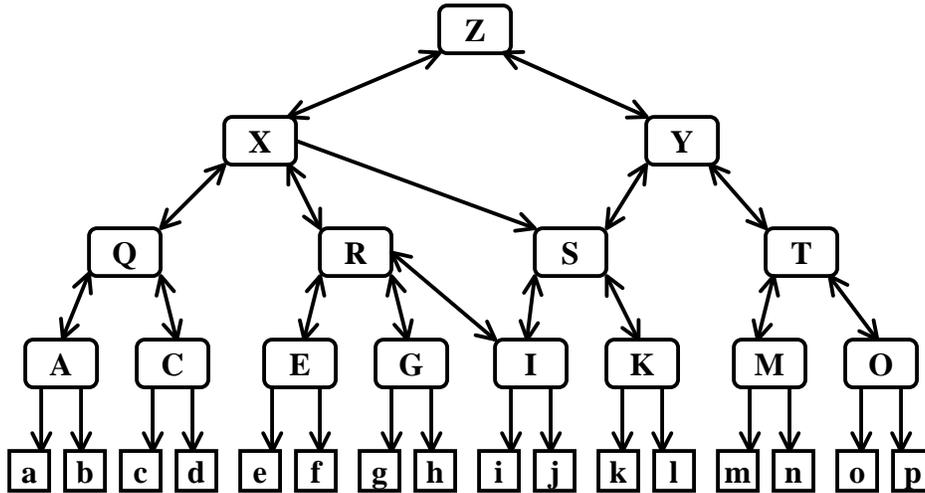
## X.509v2 CRL INNOVATIONS

- ❖ CRL distribution points
- ❖ indirect CRLs
- ❖ delta CRLs
- ❖ revocation reason
- ❖ push CRLs

## GENERAL HIERARCHICAL STRUCTURE



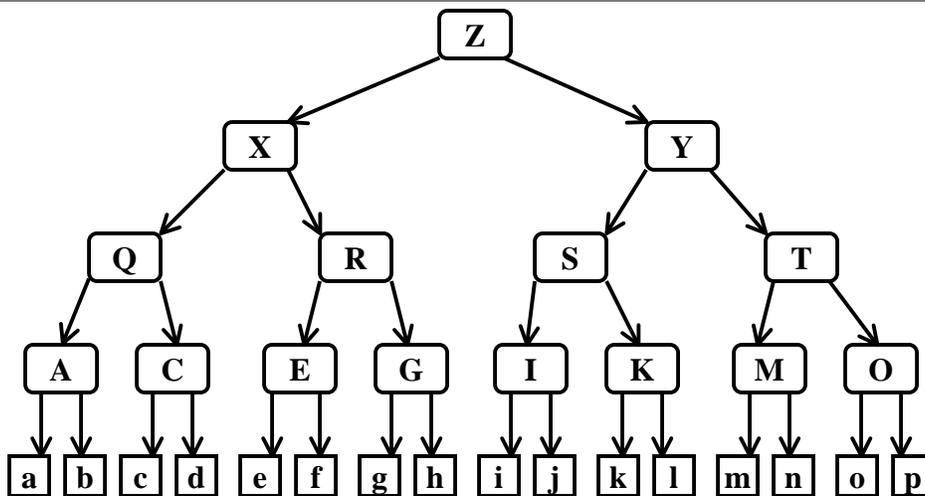
## GENERAL HIERARCHICAL STRUCTURE WITH ADDED LINKS



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## TOP-DOWN HIERARCHICAL STRUCTURE



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# FOREST OF HIERARCHIES

